

Motion In One Dimension

Particle

A particle is ideally just a piece or a quantity of matter, having practically no linear dimensions but only a position.

In practice it is difficult to get such particle, but in certain circumstances an object can be treated as particle.

Such circumstances are

(i) All the particles of solid body performing linear motion cover the same distance in the same time. Hence motion of such a body can be described in terms of the motion of its constituent particle

(ii) If the distance between two objects is very large as compared to their dimensions, these objects can be treated as particles. For example, while calculating the gravitational force between Sun and Earth, both of them can be considered as particles.

Frame of reference

A “frame of reference” is just a set of coordinates: something you use to measure the things that matter in Newtonian problems, that is to say, positions and velocities, so we also need a clock.

Or A place and situation from where an observer takes his observation is called frame of reference.

A point in space is specified by its three coordinates (x, y, z) and an “event” like, say, a little explosion, by a place and time: (x, y, z, t).

An inertial frame is defined as one in which Newton’s law of inertia holds—that is, anybody which isn’t being acted on by an outside force stays at rest if it is initially at rest, or continues to move at a constant velocity if that’s what it was doing to begin with. Example of inertial frame of reference is observer on Earth for all motion on surface of earth. Car moving with constant velocity

An example of a non-inertial frame is a rotating frame, such as a accelerating car,

Rest and Motion

When a body does not change its position with respect to time with respect to frame of reference, then it is said to be at rest. Motion is the change of position of an object with respect to time.

To study the motion of the object, one has to study the change in position (x,y,z coordinates) of the object with respect to the surroundings. It may be noted that the position of the object changes even due to the change in one, two or all the three

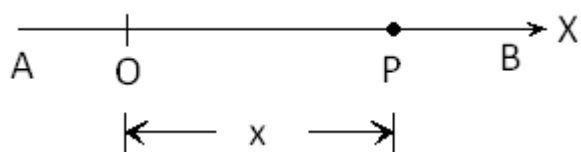
coordinates of the position of the objects with respect to time. Thus motion can be classified into three types:

(i) Motion in one dimension

Motion of an object is said to be one dimensional, if only one of coordinates specifying the position of the object changes with r

Example : An ant moving in a straight line, running athlete, etc.

Consider a particle moving on a straight line AB. For the analysis of motion we take origin. O at any point on the line and x-axis along the line. Generally we take origin at the point from where particle starts its motion and rightward direction as positive x-direction. At any moment if article is at P then its position is given by $OP = x$



(ii) Motion in two dimensions

In this type, the motion is represented by any two of the three coordinates. Example: a body moving in a plane.

(iii) Motion in three dimensions

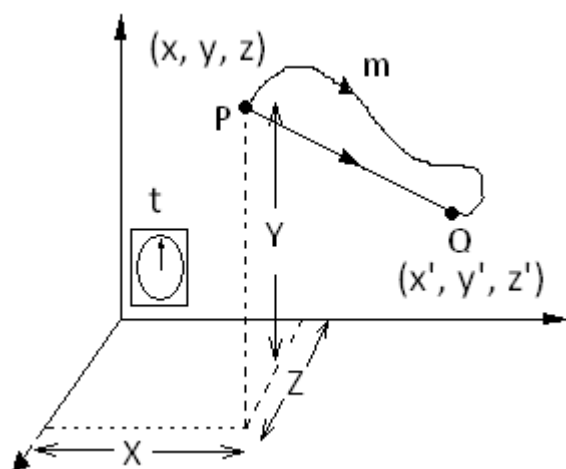
Motion of a body is said to be three dimensional, if all the three coordinates of the position of the body change with respect to time.

Examples : motion of a flying bird, motion of a satellite in the sky, motion of a molecule, etc

Position, Path-length and Displacement

POSITION

Choose a rectangular coordinate system consisting of three mutually perpendicular axes, labeled X-, Y-, and Z- axes. The point of intersection of these three axes is called origin (O) and serves as the reference point, the coordinates (x,y,x) of a particle at point P describe the position of the object with respect to this frame of reference. To measure the time we put clock in this system



If all the coordinate of particle remains unchanged with time then particle is considered at rest with respect to this frame of reference.

If position of particle at point P given by coordinates (x, y, z) at time t and particles position coordinates are (x', y', z') at time t', that is at least one coordinates of the particle is changed with time then particle is said to be in motion with respect to this frame of reference

PATH LENGTH

The path length of an object in motion in a given time is the length of actual path traversed by the object in the given time. As shown in figure actual path travelled by the particle is PmO . Path length is always positive

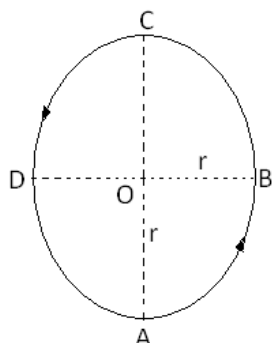
DISPLACEMENT Dimension-and-error-(Recovered)

The displacement of an object in motion in a given time is defined as the change in a position of the object, i.e., the difference between the final and initial positions of the object in a given time. It is the shortest distance between the two positions of the object and its directions is from initial to final position of the object, during the given interval of time. It is represented by the vector drawn from the initial position to its final position. As shown in figure. Since displacement is vector it may be zero, or negative also

Solved numerical

Q) A particle moves along a circle of radius r . It starts from A and moves in anticlockwise direction as shown in figure. Calculate the distance travelled by the particle and magnitude of displacement from each of following cases

(i) from A to B (ii) from A to C (iii) from A to D (iv) one complete revolution of the particle



Solution

(i) Distance travelled by particle from A to B is One fourth of circumference thus

$$\text{path length} = \frac{2\pi r}{4} = \frac{\pi r}{2}$$

Displacement

$$|AB| = \sqrt{(OA)^2 + (OB)^2} = \sqrt{r^2 + r^2} = \sqrt{2}r$$

(ii) Distance travelled by the particle from A to C is half of the circumference

$$\text{path length} = \frac{2\pi r}{2} = \pi r$$

Displacement

$$|AC| = r+r = 2r$$

(iii) Distance travelled by the particle from A to D is three fourth of the circumference

$$\text{path length} = 2\pi r \frac{3}{4} = \frac{3}{2}\pi r$$

Displacement AD

$$|AD| = \sqrt{(OA)^2 + (OD)^2} = \sqrt{r^2 + r^2} = \sqrt{2}r$$

(iv) For one complete revolution total distance is equal to circumference of circle

Path length = $2\pi r$

Since initial position and final position is same displacement is zero

Speed and velocity

Speed

It is the distance travelled in unit time. It is a scalar quantity.

$$\text{speed} = \frac{\text{path length}}{\text{time}}$$

Solved numerical

Q) A motorcyclist covers $1/3^{\text{rd}}$ of a given distance with speed 10 kmh^{-1} , the next $1/3^{\text{rd}}$ at 20 kmh^{-1} and the last $1/3^{\text{rd}}$ at of 30 kmh^{-1} . What is the average speed of the motorcycle for the entire journey

Solution:

Let total distance or path length be $3x$

Time taken for first $1/3^{\text{rd}}$ path length

$$t_1 = \frac{\text{path length}}{\text{speed}} = \frac{x}{10} \text{ hr}$$

Time taken for second $1/3^{\text{rd}}$ path length

$$t_2 = \frac{\text{path length}}{\text{speed}} = \frac{x}{20} \text{ hr}$$

Time taken for third $1/3^{\text{rd}}$ path length

$$t_3 = \frac{\text{path length}}{\text{speed}} = \frac{x}{30} \text{ hr}$$

Total time taken to travel path length of $3x$ is, $t = t_1 + t_2 + t_3$

Substituting values of t_1 , t_2 and t_3 in above equation we get

$$t = \frac{x}{10} + \frac{x}{20} + \frac{x}{30} = \frac{11x}{60} \text{ hr}$$

Form the formula for speed

$$\text{speed} = \frac{\text{path length}}{\text{time}}$$

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$$\text{speed} = \frac{3x}{\frac{11x}{60}} = \frac{180}{11} = 16.36 \text{ kmh}^{-1}$$

Velocity

The velocity of a particle is defined as the rate of change of displacement of the particle. It is also defined as the speed of the particle in a given direction. The velocity is a vector quantity. It has both magnitude and direction.

$$velocity = \frac{displacement}{time}$$

Units for velocity and speed is $m\ s^{-1}$ and its dimensional formula is LT^{-1} .

Uniform velocity

A particle is said to move with uniform velocity if it moves along a fixed direction and covers equal displacements in equal intervals of time, however small these intervals of time maybe.

Non uniform or variable velocity

The velocity is variable (non-uniform), if it covers unequal displacements in equal intervals of time or if the direction of motion changes or if both the rate of motion and the direction change.

Average velocity

Let s_1 be the position of a body in time t_1 and s_2 be its position in time t_2 . The average velocity during the time interval $(t_2 - t_1)$ is defined as

$$v = \frac{s_2 - s_1}{t_2 - t_1} = \frac{\Delta s}{\Delta t}$$

Average speed of an object can be zero, positive or zero. It depends on sign of displacement.

In general average speed of an object can be equal to or greater than the magnitude of the average velocity

Instantaneous velocity

It is the velocity at any given instant of time or at any given point of its path. The instantaneous velocity v is given by

$$v = \lim_{\Delta t \rightarrow 0} \frac{\Delta s}{\Delta t} = \frac{ds}{dt}$$

Acceleration

If the magnitude or the direction or both of the velocity changes with respect to time, the particle is said to be under acceleration. Acceleration of a particle is defined as the rate of change of velocity.

If object is performing circular motion with constant speed then also it is accelerated motion as direction of velocity is changing

Acceleration is a vector quantity.

$$acceleration = \frac{change\ in\ velocity}{time}$$

If u is the initial velocity and v , the final velocity of the particle after a time t , then the acceleration,

$$a = \frac{v - u}{t}$$

Its unit is m s^{-2} and its dimensional formula is LT^{-2}

The instantaneous acceleration is

$$a = \frac{dv}{dt} = \frac{d}{dt} \left(\frac{ds}{dt} \right) = \frac{d^2s}{dt^2}$$

If the velocity decreases with time, the acceleration is negative. The negative acceleration is called **retardation or deceleration**

Equations of motion

Motion in straight line with uniform velocity

If motion takes place with uniform velocity v on straight line the

Displacement in time t , $S = vt$ --- eq(1)

Acceleration of particle is zero

Motion in a straight line with uniform acceleration – equations of motion

Let particle moving in a straight line with velocity u (velocity at time $t = 00$ and with uniform acceleration a . Let its velocity be v at the end of the interval of time t (final velocity at time t). Let S be the displacement at the instant t acceleration a is

$$a = \frac{v - u}{t} \text{ or}$$

$$v = u + at \text{ --- eq(2)}$$

If u and a are in same direction 'a' is positive and hence final velocity v will be more than initial velocity u , velocity increases

If u and a are in opposite direction final velocity v will be less than initial velocity u . Velocity is decreasing. And acceleration is negative

Displacement during time interval $t = \text{average velocity} \times t$

$$S = \frac{v + u}{2} \times t \text{ --- eq(3)}$$

Eliminating v from equation 3 and equation 2 we get

$$S = \frac{u + at + u}{2} \times t$$

$$S = ut + \frac{1}{2}at^2 \text{ --- eq(4)}$$

Another equation can be obtained by eliminating t from equation 2 and equation 3

$$v = u + at$$

$$t = \frac{v - u}{a}$$

$$S = \frac{v + u}{2} \times \frac{v - u}{a}$$

$$S = \frac{v^2 - u^2}{2a}$$

$$v^2 = u^2 + 2aS \text{ --- eq(5)}$$

Distance transverse by the particle in n^{th} second of its motion

The velocity at the beginning of the n^{th} second = $u + a(n-1)$

The velocity at the end of n^{th} second = $u + an$

Average velocity during n^{th} second v_{ave}

$$v_{ave} = \frac{u + a(n-1) + u + an}{2}$$

$$v_{ave} = u + \frac{1}{2}a(2n-1)$$

Distance during this one second

$S_n = \text{average velocity} \times \text{time}$

$$S_n = u + \frac{1}{2}a(2n-1) \times 1$$

$$S_n = u + \frac{1}{2}a(2n-1) \text{ --- eq(6)}$$

The six equations derived above are very important and are very useful in solving problems in straight-line motion

Calculus method of deriving equation of motion

The acceleration of a body is defined as

$$a = \frac{dv}{dt}$$

$$dv = a dt$$

Integrating we get $v = at + A$

Where A is constant of integration . For initial condition $t = 0, v = u$ (initial velocity)

we get $A = u$

$\therefore v = u + at$

We know that instantaneous velocity v

$$v = \frac{ds}{dt}$$

$ds = v dt$

displacement $ds = v dt = (u + at) dt$

integrating above equation

$$S = ut + \frac{1}{2}at^2 + B$$

B is integration constant

At $t = 0, S = 0$ yields $B = 0$

$$\therefore S = ut + \frac{1}{2}at^2$$

Acceleration a

$$a = \frac{dv}{dt} = \frac{dv}{dS} \cdot \frac{dS}{dt} = v \frac{dv}{dS}$$

$$\therefore a = v \frac{dv}{dS}$$

$$adS = v \cdot dv$$

Integrating we get

$$aS = \frac{v^2}{2} + C$$

Where C is integration constant

Applying initial condition , where $S = 0, v = u$ we get

$$0 = \frac{u^2}{2} + C$$

$$\text{Or } C = -\frac{u^2}{2}$$

$$\therefore aS = \frac{v^2}{2} - \frac{u^2}{2}$$

$$v^2 = u^2 + 2aS$$

If S_1 and S_2 are the distances traversed during n seconds and $(n-1)$ seconds

$$S_1 = un + \frac{1}{2}an^2$$

$$S_2 = u(n-1) + \frac{1}{2}a(n-1)^2$$

Displacement in n^{th} second

$$S_n = S_1 - S_2$$

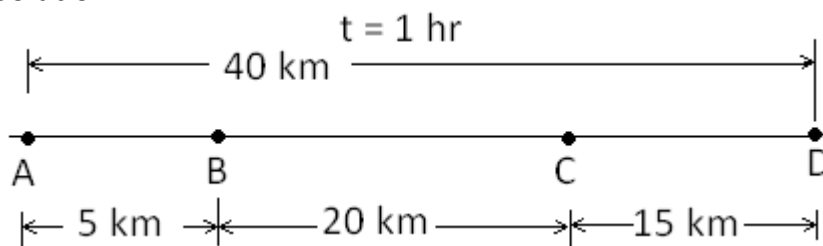
$$S_n = un + \frac{1}{2}an^2 - u(n-1) - \frac{1}{2}a(n-1)^2$$

$$S_n = u + \frac{1}{2}a(2n-1)$$

Solved numerical

Q) The distance between two stations is 40 km. A train takes 1 hour to travel this distance. The train, after starting from the first station, moves with constant acceleration for 5km, then it moves with constant velocity for 20 km and finally its velocity keeps on decreasing continuously for 15 km and it stops at the other station. Find the maximum velocity of the train.

Solution:



Motion is divided in three parts

Motion between point A and B is with constant acceleration

Here initial velocity $u = 0$ and final velocity at point B = v_{max}

Let time interval be t_1

From equation

$$S = \frac{v + u}{2} \times t$$

$$5 = \frac{v_{max} + 0}{2} \times t_1$$

$$t_1 = \frac{10}{v_{max}}$$

Motion between point B and C is with constant velocity v_{max}

Let time period t_2

Form formula $S = vt$

$$20 = v_{max} t_2$$

$$t_2 = \frac{20}{v_{max}}$$

Motion between point C and D is with retardation

Initial velocity is v_{max} and final velocity $v = 0$ let time interval t_3

From formula

$$S = \frac{v + u}{2} \times t$$

$$15 = \frac{0 + v_{max}}{2} \times t_3$$

$$t_3 = \frac{30}{v_{max}}$$

Total time taken is 1 hr

$$T = t_1 + t_2 + t_3$$

$$1 = \frac{10}{v_{max}} + \frac{20}{v_{max}} + \frac{30}{v_{max}}$$

$$\therefore v_{max} = 60 \text{ km h}^{-1}$$

Q) A certain automobile manufacturer claims that its sports car will accelerate from rest to a speed of 42.0 m/s in 8.0 s. under the important assumption that the acceleration is constant

(i) Determine the acceleration

(ii) Find the distance the car travels in 8s

(iii) Find the distance travelled in 8th s

Solution

(a) Here initial velocity $u = 0$ and final velocity $v = 42 \text{ m/s}$

From formula

$$a = \frac{v - u}{t}$$

$$a = \frac{42 - 0}{8} = 5.25 \text{ ms}^{-2}$$

(b) Distance travelled in 8.0s

From formula

$$S = ut + \frac{1}{2}at^2$$

$$S = (0)(t) + \frac{1}{2}(5.25)(8)^2 = 168 \text{ m}$$

(c) distance travelled in 8th second.

From formula

$$S_n = u + \frac{1}{2}a(2n - 1)$$

$$S_n = 0 + \frac{1}{2}(5.25)(2 \times 8 - 1) = 39.375 \text{ m}$$

Q) Motion of a body along a straight line is described by the equation

$x = t^3 + 4t^2 - 2t + 5$ where x is in meter and t in seconds

(a) Find the velocity and acceleration of the body at $t = 4\text{s}$

(b) Find the average velocity and average acceleration during the time interval from $t = 0$ to $t = 4 \text{ s}$

Solution

(a) We have to find instantaneous velocity at $t = 4\text{s}$

$$v = \frac{dx}{dt} = \frac{d}{dt}(t^3 + 4t^2 - 2t + 5)$$

$$v = \frac{d}{dt}t^3 + 4\frac{d}{dt}t^2 - 2\frac{d}{dt}t + \frac{d}{dt}5$$

$$v = 3t^2 + 4 \times 2t - 2$$

$$v = 3t^2 + 8t - 2$$

Thus we get equation for velocity, by substituting $t = 4$ in above equation we get instantaneous velocity at $t = 4$

$$v = 3(4)^2 + 8(4) - 2$$

$$v = 78 \text{ m/s}$$

To find instantaneous acceleration at $t = 4\text{s}$

$$a = \frac{dv}{dt} = \frac{d}{dt}(3t^2 + 8t - 2)$$

$$a = 6t + 8$$

Thus we get equation for acceleration, by substituting $t=4$ in equation for acceleration we get instantaneous acceleration $t=4$

$$a = 6(4) + 8$$

$$a = 32 \text{ m s}^{-2}$$

(b) Average velocity

Final position of object at time $t = 4$ s

$$X_4 = (4)^3 + 4(4)^2 - 2(4) + 5 = 125$$

Initial position of object at time $t = 0$ s

$$X_0 = (0)^3 + 4(0)^2 - 2(0) + 5 = 5$$

Displacement = $125 - 5 = 120$ m, time interval $t = 4$ seconds

Average velocity = Displacement / time = $120/4 = 30 \text{ ms}^{-1}$

Average acceleration

Initial velocity $t = 0$ from equation for velocity

$$v = 3t^2 + 8t - 2$$

$$v = 3(0)^2 + 8(0) - 2 = -2 \text{ ms}^{-1}$$

\therefore Initial velocity $u = -2 \text{ ms}^{-1}$

Final velocity is calculated as 78 ms^{-1}

From formula for average acceleration

$$a = \frac{v - u}{t} = \frac{78 - (-2)}{4} = 20 \text{ ms}^{-2}$$

Q) A particle moving in a straight line has an acceleration of $(3t - 4) \text{ ms}^{-2}$ at time t seconds. The particle is initially 1m from O, a fixed point on the line, with a velocity of 2 ms^{-1} . Find the time when the velocity is zero. Find the displacement of particle from O when $t = 3$

Solution:

$$a = \frac{dv}{dt}$$

$$\frac{dv}{dt} = 3t - 4$$

$$\Rightarrow \int_2^v dv = \int_0^t (3t - 4) dt$$

$$\Rightarrow v - 2 = \frac{3t^2}{2} - 4t$$

$$\Rightarrow v = \frac{3t^2}{2} - 4t + 2$$

The velocity will be zero when

$$\frac{3t^2}{2} - 4t + 2 = 0$$

i.e when

$$(3t - 2)(t - 2) = 0$$

$$t = \frac{2}{3} \text{ or } 2$$

Using

$$\frac{ds}{dt} = v$$

We have

$$\frac{ds}{dt} = \frac{3t^2}{2} - 4t + 2$$

$$\Rightarrow \int_1^s ds = \int_0^3 \left(\frac{3t^2}{2} - 4t + 2 \right) dt$$

$$\Rightarrow s - 1 = \left[\frac{3t^2}{2} - 4t + 2 \right]_0^3 = 1.5$$

$$\Rightarrow s = 2.5 \text{ m}$$

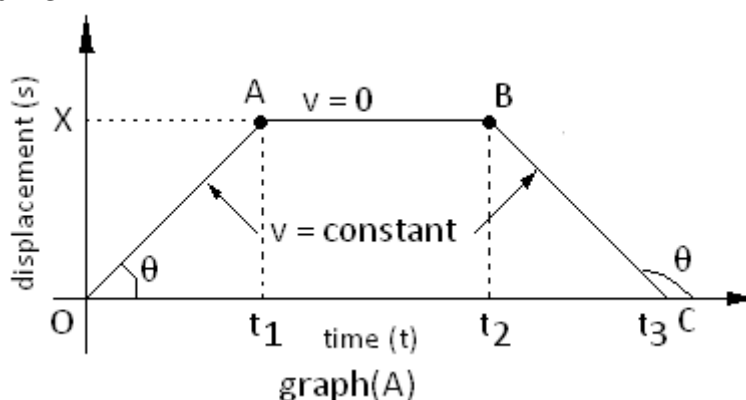
Therefore the particle is 2.5 m from O when $t = 3\text{s}$

Graphical representation of motion

(1) Displacement – time graph:

If displacement of a body is plotted on Y-axis and time on X-axis, the curve obtained is called displacement-time graph.

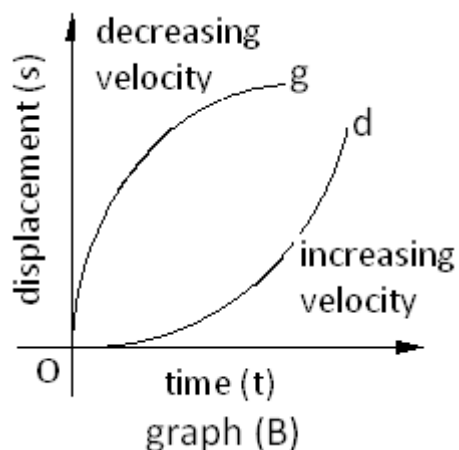
The instantaneous velocity at any given instant can be obtained from the graph by finding the slope of the tangent at the point corresponding to the time



In graph(A) object started to move with constant velocity ($a = 0$) at time $t = 0$ from origin. Object is going away represented by OA, at time t_1 object reach position X, note slope of graph AO is positive and constant.

For time period t_1 to t_2 object have not changed its position thus velocity is zero. Slope of graph is zero

For time period t_2 to t_3 object started to move towards its original position at time t_2 and reaches original position at time t_3 . Here velocity is constant ($a=0$) as slope of graph is constant. And reaching original position as slope is negative



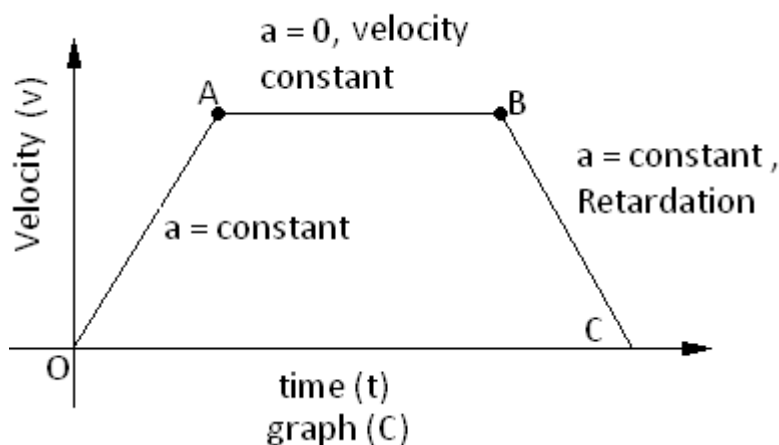
In graph(B) motion represented by Og is decelerated motion as slope is decreasing with time, hence velocity is decreasing. However object is moving away from origin

Motion represented by Od is accelerated as slope is continuously increasing with time, it indicates that velocity is increasing or acceleration is positive, object is moving away from origin

(2)Velocity-time graph

If Velocity of a body is plotted on Y-axis and time on X-axis, the curve obtained is called velocity-time graph.

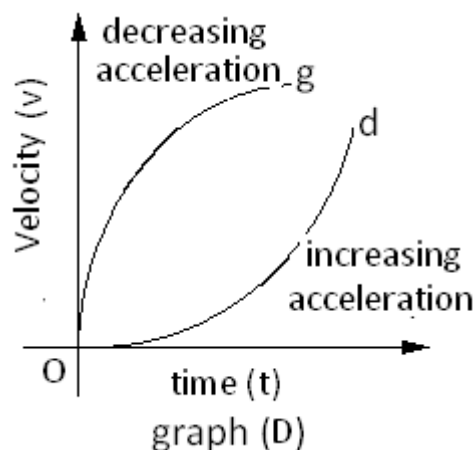
The instantaneous acceleration at any given instant can be obtained from the graph by finding the slope of the tangent at the point corresponding to the time



Graph AB is parallel straight indicate object is moving with constant velocity or acceleration is zero

Graph OA is oblique straight line slope is positive indicate object is uniformly accelerated

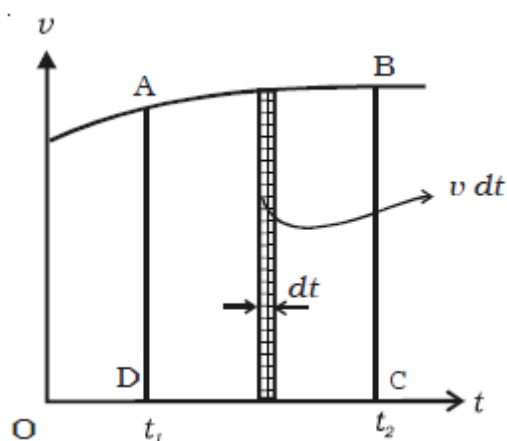
Graph BC is oblique straight line slope is negative indicated object is uniformly decelerated



Graph Og represents decreasing acceleration as slop is decreasing with time

Graph Od represent increasing acceleration as slop is increasing with time

When the velocity of the particle is plotted as a function of time, it is velocity-time graph. Area under the curve gives displacement



We know that

$$v = \frac{dS}{dt}$$

$$dS = v \cdot dt$$

If displacements are S_1 and S_2 at time t_1 and t_2 then

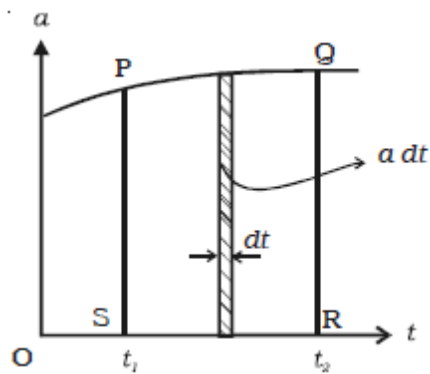
$$\int_{S_1}^{S_2} dS = \int_{t_1}^{t_2} v dt$$

$$S_2 - S_1 = \int_{t_1}^{t_2} v dt = \text{Area } ABCD$$

The area under the $v - t$ curve, between the given intervals of time, gives the change in displacement or the distance travelled by the particle during the same interval.

Acceleration – time graph

When the acceleration is plotted as a function of time, it is acceleration - time graph



$$a = \frac{dv}{dt}$$

$$dv = a dt$$

If v_1 and v_2 are the velocities at time t_1 and t_2 then

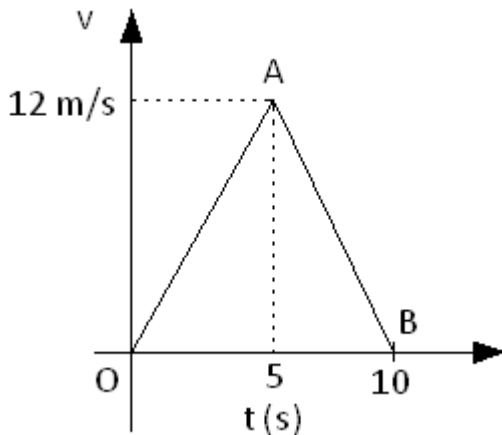
$$\int_{v_1}^{v_2} dy = \int_{t_1}^{t_2} a dt$$

$$v_2 - v_1 = \int_{t_1}^{t_2} a dt = \text{AreaPQRS}$$

The area under the $a - t$ curve, between the given intervals of time, gives the change in velocity of the particle during the same interval. If the graph is parallel to the time axis, the body moves with constant acceleration.

Solved numerical

Q) The $v - t$ graph of a particle moving in straight line is shown in figure. Obtain the distance travelled by the particle from (a) $t = 0$ to $t = 10$ s and from (b) $t = 2$ s to $t = 6$ s



Solution:

(a) Distance travelled in time period $t = 0$ to $t = 10$ s is area of triangle OAB = $(1/2) \times 10 \times 12 = 60$ m

(b) Distance in time period $t = 2$ to $t = 6$ s

From graph slope of line OA is 2.4 m/s^2

Initial velocity at $t = 2$ sec $u = 4.8$ thus using formula

$X = ut + (1/2)at^2$ here time period is 3 sec

$$X_1 = (4.8)(3) + (1/2)(2.4)(3)^2 = 25.2$$

For segment A to B acceleration is 2.4 time period 1 s $u = 5$

$$X_2 = (12)(1) - (1/2)(2.4)(1)^2 = 10.8$$

Thus distance = $25.2 + 10.8 = 36$ m

Vertical motion under gravity

When an object is thrown vertically upward or dropped from height, it moves in a vertical straight line. If the air resistance offered by air to the motion of the object is

neglected, all objects moving freely under gravity will be acted upon by its weight only

This causes vertical acceleration g having value 9.8 m/s^2 , so the equation for motion in a straight line with constant acceleration can be used.

In some problems it is convenient to take the downward direction of acceleration as positive, in such case if the object is moving upward initial velocity should be taken as negative and displacement positive.

If object is moving downwards then, initial velocity should be taken as positive and displacement negative.

Projection of a body vertically upwards

Suppose an object is projected upwards from point A with velocity u

If we take downward direction of g as **Negative** then

- (i) At a time t its velocity $v = u - gt$
- (ii) At a time t , its displacement from A is given by
 $S = ut - (1/2)gt^2$
- (iii) Its velocity when its displacement S is given by
 $v^2 = u^2 - 2gS$
- (iv) When it reaches the maximum height, its velocity $v = 0$.

This happens when $t = u/g$. The body is instantaneously rest

From formula

$$V = u - gt$$

$$t = v/g$$

- (v) The maximum height reached. At maximum height final velocity $v = 0$ and $S = H$ thus

From equation

$$v^2 = u^2 - 2gS$$

$$0 = u^2 - 2gH$$

$$H = \frac{u^2}{2g}$$

- (vi) Total time to go up and return to the point of projection

Displacement $S = 0$ Thus from formula

$$S = ut - (1/2)gt^2$$

$$0 = ut - (1/2)gt^2$$

$$T = 2u/g$$

- (vii) At any point C between A and B, where $AC = s$, the velocity v is given by

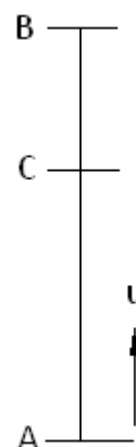
$$v = \pm\sqrt{u^2 - 2gS}$$

The velocity of body while crossing C upwards =

$$v = +\sqrt{u^2 - 2gS}$$

The velocity of body while crossing C downwards

$$v = -\sqrt{u^2 - 2gS}$$



Magnitudes of velocities are same

Solved numerical

Q) A body is projected upwards with a velocity 98 m/s.

Find (a) the maximum height reached

(b) the time taken to reach maximum height

(c) its velocity at height 196 m from the point of projection

(d) velocity with which it will cross down the point of projection and

(e) the time taken to reach back the point of projection

Solution:

(a) Maximum height

$$H = \frac{u^2}{2g} = \frac{(98)^2}{2 \times 9.8} = 490 \text{ m}$$

(b) Time taken to reach maximum height

$$T = u/g = 9.8/9.8 = 10\text{s}$$

(c) Velocity at a height of 196 m from the point of projection

$$v = \pm\sqrt{u^2 - 2gS}$$

$$v = \pm\sqrt{(98)^2 - 2(9.8)(196)} = \pm 75.91 \text{ m/s}$$

+75.91 m/s while crossing the height upward and -75.91 m/ while crossing it downwards

(d) Velocity with which it will cross down the point of projection

Magnitude is same but direction is opposite hence $V = -u = -98 \text{ m/s}$

(e) The time taken to reach back the point of projection

$$T = 2u/g = (2 \times 98)/9.8 = 20 \text{ s}$$

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